Abstract

In many domains, relationships between categories are encoded in the knowledge graph. Recently, promising results have been achieved by incorporating knowledge graph as side information in hard classification tasks with severely limited data. However, prior models consist of highly complex architectures with many sub-components that all seem to impact performance. In this paper, we present a comprehensive empirical study on graph embedded few-shot learning. We introduce a graph regularization approach that allows a deeper understanding of the impact of incorporating graph information between labels. Our proposed regularization is widely applicable and model-agnostic, and boosts the performance of any few-shot learning model, including fine-tuning, metric-based and optimization-based meta-learning. Our approach improves performance of strong base learners by up to 2% on Mini-ImageNet and 6.7% on ImageNet-FS, outperforming state-of-the-art graph embedded methods. Additional analyses reveal that graph regularizing models results in a lower loss for more difficult tasks, such as those with fewer shots and less informative support examples.

1 Introduction

Few-shot learning refers to the task of generalizing from a very few examples, an ability that humans have but machines lack. Recently, major breakthroughs have been achieved with meta-learning, which leverages prior experience from many related tasks to effectively learn to adapt to unseen tasks [2, 24]. At a high level, meta-learning has been divided into metric-based approaches that learn a transferable metric across tasks [25, 26, 29], and optimization-based approaches that learn initializations for fast adaptation on new tasks [6, 22]. Beyond meta-learning, transfer learning by pretraining and fine-tuning on novel tasks has achieved surprisingly competitive performance on few-shot tasks [4, 5, 31].

In many domains, external knowledge about the class labels can be used. For example, this information is crucial in the zero-shot learning paradigm, which seeks to generalize to novel classes without
Recent few-shot learning methods have been enhanced with graph information, achieving state-of-the-art performance on benchmark image classification tasks [3, 13, 14, 15, 27]. Proposed methods typically employ sophisticated and highly parameterized graph models on top of convolutional feature extractors. However, the complexity of these methods prevents deeper understanding of the impact of incorporating graph information. Furthermore, these models are inflexible and incompatible with other approaches in the rapidly-improving field of meta-learning, demonstrating the need for a model-agnostic graph augmentation method.

Here, we conduct a comprehensive empirical study of incorporating knowledge graph information into few-shot learning. First, we introduce a graph regularization approach for incorporating graph relationships between labels applicable to any few-shot learning method. Motivated by node embedding [7] and graph regularization principles [8], our proposed regularization enforces category-level relationships to preserve neighborhood similarities in a graph. By design, it allows us to directly measure benefits of enhancing few-shot learners with graph information. We incorporate our proposed regularization into three major approaches of few-shot learning: (i) metric-learning, represented by Prototypical Networks [25], (ii) optimization-based learning, represented by LEO [22], and (iii) fine-tuning, represented by SGM [21] and S2M2 [17]. We demonstrate that graph regularization consistently improves each method and can be widely applied whenever category relations are available. Next, we compare our approach to state-of-the-art methods, including those that utilize the same category hierarchy on standard benchmark Mini-ImageNet and large-scale ImageNet-FS datasets. Remarkably, we find that our approach improves the performance of strong base learners by as much as 6.7% and outperforms graph embedded baselines, even though it is simple, easy to tune, and introduces minimal additional parameters. Finally, we explore the behavior of incorporating graph information in controlled synthetic experiments. Our analysis shows that graph regularizing models yields better decision boundaries in lower-shot learning, and achieves significantly higher gains on more difficult few-shot episodes.

2 Model-Agnostic Graph Regularization

Our approach is a model-agnostic graph regularization objective that is based on the idea that the graph structure of class labels can guide learning of model parameters. The graph regularization objective ensures labels in the same graph neighborhood have similar parameters. The regularization is combined with a classification loss to form the overall objective. The classification loss is flexible and depends on the base learner. For instance, the classification loss can correspond to cross-entropy loss [4], or distance-based loss between example embeddings and class prototypes [25].

2.1 Problem Setup

We assume that we are given a dataset defined as a pair of examples $X \subseteq \mathcal{X}$ with corresponding labels $Y \subseteq \mathcal{Y}$. We say that point $x_i \in X$ has the label $y_i \in Y$. For each episode, we learn from a support set $D_s = \{(x_1, y_1), (x_2, y_2), ..., (x_K, y_K)\}$ and evaluate on a held-out query set $D_q = \{(x_1^q, y_1^q), (x_2^q, y_2^q), ..., (x_T^q, y_T^q)\}, D_q \cap D_s = \emptyset$. For each dataset, we split all classes into $C_{\text{train}}$ and $C_{\text{test}}, C_{\text{train}} \cap C_{\text{test}} = \emptyset$. During evaluation, we sample the $N$ classes from a larger set of classes $C_{\text{test}}$, and sample $K$ examples from each class. During training, we use a disjoint set of classes $C_{\text{train}}$ to train the model. Non-episodic training approaches treat $C_{\text{train}}$ as a standard supervised learning problem, while episodic training approaches match the conditions on which the model is trained and evaluated by sampling episodes from $C_{\text{train}}$. More details on the problem setup can be found in Appendix A. Additionally, we assume that there exists side information about the labels in the form of a graph $G(\mathcal{Y}, E)$ where $\mathcal{Y}$ is the set of all nodes in the label graph, and $E$ is the set of edges.

2.2 Regularization

We incorporate graph information using the random walk-based node2vec objective [7]. Random walk methods for graph embedding [20] are fit by maximizing the probability of predicting the
neighbors for each target node in the graph. Node2vec performs biased random walks by introducing hyperparameters to balance between breadth-first search (BFS) and depth-first search (DFS) to capture local structures and global communities. We formulate the node2vec loss below:

\[
L_{\text{graph}}(G, \theta) = -\sum_{y \in Y} \left[ -\log Z_y + \sum_{n \in N(y)} \frac{1}{T} \text{sim}(\theta_n, \theta_y) \right],
\]

where \( \theta \) are node representations, \( \text{sim} \) is a similarity function between the nodes, \( N(y) \) is the set of neighbor nodes of node \( y \), \( T \) is the temperature hyperparameter, and \( Z_y \) is partition function defined as \( Z_y = \sum_{n \in \mathcal{Y}} \exp \left[ \frac{1}{T} \sum_{n \in N(y)} \text{sim}(\theta_n, \theta_y) \right] \). The partition function is approximated using negative sampling [18]. We obtain the neighborhood \( N(y) \) by performing a random walk starting from a source node \( y \). The similarity function \( \text{sim} \) depends on the base learner, which we outline in Section 2.3.

### 2.3 Augmentation Strategies

Our graph-regularization framework is model-agnostic and intuitively applicable to a wide variety of few-shot approaches. Here, we describe augmentation strategies for high-performing learners from metric-based meta-learning, optimization-based meta-learning and fine-tuning by formulating each as a joint learning objective.

#### 2.3.1 Augmenting Metric-Based Models

Metric-based approaches learn an embedding function to compare query set examples. Prototypical networks are a high-performing learner of this class, especially when controlling for model complexity [4, 28]. Prototypical networks construct a prototype \( p_j \) of the \( j^{th} \) class by taking the mean of support set examples, and comparing query examples using Euclidean distance. We regularize these prototypes so they respect class similarities and get the joint objective:

\[
\sum_{(x_i, y_i) \in \mathcal{D}_s} \left[ ||x_i - p_{y_i}||^2_2 + \sum_{y' \in Y} \exp(-||x_i - p_{y'}||^2_2) \right] + \lambda L_{\text{graph}}(G, \theta).
\]

We set the graph similarity function to negative Euclidean distance, \( \text{sim}(p_i, p_j) = -||p_i - p_j||^2_2 \). Note that our approach can easily be extended to other metric-based learners, for example regularizing the output of the relation module for Relation Networks [26].

#### 2.3.2 Augmenting Optimization-Based Models

Optimization-based meta-learners such as MAML [6] and LEO [22] consist of two optimization loops: the outer loop updates the neural network parameters to an initialization that enables fast adaptation, while the inner loop performs a few gradient updates over the support set to adapt to the new task. Graph regularization enforces class similarities among parameters during inner-loop adaptation.

Specifically for LEO, we pass support set examples through an encoder to produce latent class encodings \( z \), which are decoded to generate classifier parameters \( \theta \). Given instantiated model parameters learned from the outer loop, gradient steps are taken in the latent space to get \( z' \) while freezing all other parameters to produce final adapted parameters \( \theta' \). For more details, please refer to [22]. Concretely, we obtain the joint regularized objective below for the inner-loop adaptations:

\[
\sum_{(x_i, y_i) \in \mathcal{D}_s} \left[ -z^T y_i x_i + \sum_{y' \in Y} \exp(z_{y_i}^T x_i) \right] + \lambda L_{\text{graph}}(G, z).
\]

We set the graph similarity function to the inner product, \( \text{sim}(z_i, z_j) = z_i^T z_j \), though in practice cosine similarity, \( \text{sim}(z_i, z_j) = z_i^T z_j / ||z_i|| ||z_j|| \) results in more stable learning.

#### 2.3.3 Augmenting Fine-tuning Models

Recent approaches such as Baseline++ [4] and S2M2N [17] have demonstrated remarkable performance by pre-training a model on the training set, and fine-tuning the classifier parameters \( \theta \) on the
support set of each task. We follow [4] and freeze the feature embedding model during fine-tuning, though the model can be fine-tuned as well [5]. We perform graph regularization on the classifiers in the last layer of the network, which are learned for novel classes during fine-tuning. This results in the objective below:

$$\sum_{(x_i, y_i) \in D_s} - \frac{x_i^T \theta_{y_i}}{||x_i|| ||\theta_{y_i}||} + \sum_{y' \in \mathcal{Y}} \exp \left( \frac{x_i^T \theta_{y_i}}{||x_i|| ||\theta_{y_i}||} \right) + \lambda L_{graph}(G, \theta).$$  \hspace{1cm} (4)

We set the graph similarity to cosine similarity,

$$sim(\theta_i, \theta_j) = \frac{\theta_i^T \theta_j}{||\theta_i|| ||\theta_j||}.$$

3 Experimental Results

For all ImageNet experiments, we use the associated WordNet [19] category hierarchy to define graph relationships between classes. Details of the experimental setup are given in Appendix B. On the synthetic dataset, we analyze the effect of graph regularizing few-shot methods.

3.1 Mini-ImageNet Experiments

We compare performance to few-shot baselines and graph embedded approach KGTN [3] on the Mini-Imagenet experiment. We enhance S2M2\(_R\) [17], a strong baseline fine-tuning model. Table 1 shows graph regularization results on Mini-ImageNet compared to results of the state-of-the-art models. We find that S2M2\(_R\) enhanced with the proposed graph regularization outperforms all other methods on both 1- and 5-shot tasks. As an additional baseline, we consider KGTN which also utilizes the WordNet hierarchy for better generalization. To ensure that our improvements are not caused by the embedding function, we pretrain KGTN feature extractor using S2M2\(_R\). Even when controlling for improvements in the feature extractor, we find that our our simple graph regularization method outperforms complex graph-embedded model.

Table 1: Results on 1-shot and 5-shot classification on the Mini-ImageNet dataset. We report average accuracy over 600 randomly sampled episodes. We show graph-based models in the bottom section.

<table>
<thead>
<tr>
<th>Model</th>
<th>Backbone</th>
<th>1-shot</th>
<th>5-shot</th>
</tr>
</thead>
<tbody>
<tr>
<td>Qiao [21]</td>
<td>WRN 28-10</td>
<td>59.60 ± 0.41</td>
<td>73.74 ± 0.19</td>
</tr>
<tr>
<td>Baseline++ [4]</td>
<td>WRN 28-10</td>
<td>59.62 ± 0.81</td>
<td>78.80 ± 0.61</td>
</tr>
<tr>
<td>LEO (train+val) [22]</td>
<td>WRN 28-10</td>
<td>61.76 ± 0.08</td>
<td>77.59 ± 0.12</td>
</tr>
<tr>
<td>ProtoNet [25]</td>
<td>WRN 28-10</td>
<td>62.60 ± 0.20</td>
<td>79.97 ± 0.14</td>
</tr>
<tr>
<td>MatchingNet [29]</td>
<td>WRN 28-10</td>
<td>64.03 ± 0.20</td>
<td>76.32 ± 0.16</td>
</tr>
<tr>
<td>S2M2(_R) [17]</td>
<td>WRN 28-10</td>
<td>64.93 ± 0.18</td>
<td>83.18 ± 0.11</td>
</tr>
<tr>
<td>SimpleShot [31]</td>
<td>WRN 28-10</td>
<td>65.87 ± 0.20</td>
<td>82.09 ± 0.14</td>
</tr>
<tr>
<td>KGTN [3]</td>
<td>WRN 28-10</td>
<td>65.71 ± 0.75</td>
<td>81.07 ± 0.50</td>
</tr>
<tr>
<td>S2M2(_R) + Graph (Ours)</td>
<td>WRN 28-10</td>
<td><strong>66.93 ± 0.65</strong></td>
<td><strong>83.35 ± 0.53</strong></td>
</tr>
</tbody>
</table>

3.2 Graph Regularization is Model-Agnostic

We augment ProtoNet [25], LEO [22], and S2M2\(_R\) [17] approaches with graph regularization and evaluate effectiveness of our approach on the Mini-ImageNet dataset. These few-shot learning models are fundamentally different and vary in both optimization and training procedures. For example, ProtoNet and LEO are both trained episodically, while S2M2\(_R\) is trained non-episodically. However, the flexibility of our graph regularization loss allows us to easily extend each method. Table 2 shows the results of graph enhanced few-shot baselines. The results demonstrate that graph regularization consistently improves performance of few-shot baselines with larger gains in the 1-shot setup.
Table 2: Performance of graph-regularized few-shot baselines on the Mini-ImageNet dataset. We report average accuracy over 600 randomly sampled episodes.

<table>
<thead>
<tr>
<th>Model</th>
<th>Backbone</th>
<th>1-shot</th>
<th>5-shot</th>
</tr>
</thead>
<tbody>
<tr>
<td>ProtoNet [25]</td>
<td>ResNet-18</td>
<td>54.16 ± 0.82</td>
<td>73.68 ± 0.65</td>
</tr>
<tr>
<td>ProtoNet + Graph (Ours)</td>
<td>ResNet-18</td>
<td><strong>55.47 ± 0.73</strong></td>
<td><strong>74.56 ± 0.49</strong></td>
</tr>
<tr>
<td>LEO (train) [22]</td>
<td>WRN 28-10</td>
<td>58.22 ± 0.09</td>
<td>74.46 ± 0.19</td>
</tr>
<tr>
<td>LEO + Graph (Ours)</td>
<td>WRN 28-10</td>
<td><strong>60.93 ± 0.19</strong></td>
<td><strong>76.33 ± 0.17</strong></td>
</tr>
<tr>
<td>S2M2R [17]</td>
<td>WRN 28-10</td>
<td>64.93 ± 0.18</td>
<td>83.18 ± 0.11</td>
</tr>
<tr>
<td>S2M2R + Graph (Ours)</td>
<td>WRN 28-10</td>
<td><strong>66.93 ± 0.65</strong></td>
<td><strong>83.35 ± 0.53</strong></td>
</tr>
</tbody>
</table>

3.3 Large-Scale Few-Shot Classification

We next evaluate our graph regularization approach on the large-scale ImageNet-FS dataset, which includes 1000 classes. Notably, this task is more challenging because it requires choosing among all novel classes, an arguably more realistic evaluation procedure. We sample $K$ images per category, repeat the experiments 5 times, and report mean accuracy with 95% confidence intervals. Results demonstrate that our graph regularization method boosts performance of the SGM baseline [9] by as much as 6.7%. Remarkably, augmenting SGM with graph regularization outperforms all few-shot baselines, as well as models that benefit from class semantic information and label hierarchy such as KTCH [16] and KGTN [3]. We include further experimental details in Appendix B, and explore further ablations to justify design choices in Appendix C.

Table 3: Top-5 accuracy on the novel categories for the Imagenet-FS dataset. KTCH and KGTN are graph-based models. We report 95% confidence intervals where provided. The 95% confidence intervals for [9, 25, 29, 32] are on the order of 0.2%.

<table>
<thead>
<tr>
<th>Model</th>
<th>Backbone</th>
<th>1-shot</th>
<th>2-shot</th>
<th>5-shot</th>
</tr>
</thead>
<tbody>
<tr>
<td>SGM [9]</td>
<td>ResNet-50</td>
<td>54.3</td>
<td>67.0</td>
<td>77.4</td>
</tr>
<tr>
<td>MatchingNet [29]</td>
<td>ResNet-50</td>
<td>53.5</td>
<td>63.5</td>
<td>72.7</td>
</tr>
<tr>
<td>ProtoNet [25]</td>
<td>ResNet-50</td>
<td>49.6</td>
<td>64.0</td>
<td>74.4</td>
</tr>
<tr>
<td>PMN [32]</td>
<td>ResNet-50</td>
<td>53.3</td>
<td>65.2</td>
<td>75.9</td>
</tr>
<tr>
<td>KTCH [16]</td>
<td>ResNet-50</td>
<td>58.1</td>
<td>67.3</td>
<td>77.6</td>
</tr>
<tr>
<td>KGTN [3]</td>
<td>ResNet-50</td>
<td>60.1</td>
<td>69.4</td>
<td>78.1</td>
</tr>
<tr>
<td>SGM + Graph (Ours)</td>
<td>ResNet-50</td>
<td><strong>61.09 ± 0.37</strong></td>
<td><strong>70.35 ± 0.17</strong></td>
<td><strong>78.61 ± 0.19</strong></td>
</tr>
</tbody>
</table>

3.4 Synthetic Experiments

To analyze the benefits of graph regularization, we devise a few-shot classification problem on a synthetic dataset. We first embed a balanced binary tree of height $h$ in $d$-dimensions using node2vec [7]. We set all leaf nodes as classes, and assign half as base and half as novel. For each task, we sample $k$ support and $q$ query examples from a Gaussian with mean centered at each class embedding and standard deviation $\sigma$. Given $k$ support examples, the task is to predict the correct class for query examples among novel classes. In these experiments, we set $d = 4$, $h \in \{4, 5, 6, 7\}$, $k \in \{1, 2, \ldots, 10\}$, $q = 50$, and $\sigma \in \{0.1, 0.2, 0.4\}$. The baseline model is a linear classifier layer with cross-entropy loss, and we apply graph regularization to this baseline. We learn using SGD with learning rate 0.1 for 100 iterations.

We first visualize the learned decision boundaries on identical tasks with and without graph regularization in Figure 1. In this task, the sampled support examples are far away from the query examples, particularly for the purple and green classes. The baseline model learns poor decision boundaries, resulting in many misclassified query examples. In contrast, much fewer query examples are misclassified when graph regularization is applied. Intuitively, graph regularization helps more when the support set is further away from the sampled data points, and thus generalization is harder.
To measure the relationship between few-shot task difficulty and performance, we adopt the hardness metric proposed in [5]. Intuitively, few-shot task hardness depends on the relative location of labeled and unlabeled examples. If labeled examples are close to the unlabeled examples of the same class, then learned classifiers will result in good decision boundaries and consequently accuracy will be high. Given a support set $D_s$ and query set $D_q$, the hardness $\Omega_\phi$ is defined as the average log-odds of a query example being classified incorrectly:

$$\Omega_\phi(D_q; D_s) = \frac{1}{N_q} \sum_{(x, y) \in D_q} \log \frac{1 - p(y|x)}{p(y|x)}$$

where $p(\cdot|x_i)$ is a softmax distribution over $\text{sim}(x_i, p_j) = -||x_i - p_j||^2_2$, the similarity scores between query examples $x_i$ and the means of the support examples $p_j$ from the $j^{th}$ class in $D_s$.

We show average loss with shaded 95% confidence intervals across shots in Figure 2 (left), confirming our observations in real-world datasets that graph regularization improves the baseline model the most for tasks with lower shots. Furthermore, using our synthetic dataset, we artificially create more difficult few-shot tasks by increasing $h$, tree heights, and increasing $\sigma$, the spread of sampled examples. We plot loss with respect to the proposed hardness metric of each task in Figure 2 (right). The results demonstrate that graph regularization achieves higher performance gains on more difficult tasks.

Figure 1: Synthetic experiment results. PCA visualization of learned classifiers for a single task without (left) and with graph regularization (right). Support examples are squares, query examples are dots, learned classifiers are crosses. Shaded regions show decision boundaries.

Figure 2: Quantified results of classification loss across shots (left) and task hardness metric (right). Each point is a sampled task. Red color denotes graph regularized method and gray method without graph regularization.
4 Conclusion

We have introduced a graph regularization method for incorporating label graph side-information into few-shot learning. Our approach is simple and effective, model-agnostic and boosts performance of a wide range of few-shot learners. We further showed that introduced graph regularization outperforms more complex state-of-the-art graph embedded models.

Acknowledgments and Disclosure of Funding

We thank Yueming Wang and Eli Pugh for discussions and providing feedback on our manuscript. We also gratefully acknowledge the support of DARPA under Nos. FA865018C7880 (ASED), N660011924033 (MCS); ARO under Nos. W911NF-16-1-0342 (MURI), W911NF-16-1-0171 (DURIP); NSF under Nos. OAC-1835598 (CINES), OAC-1934578 (HDR), CCF-1918940 (Expeditions), IIS-2030477 (RAPID); Stanford Data Science Initiative, Wu Tsai Neurosciences Institute, Chan Zuckerberg Biohub, Amazon, Boeing, JPMorgan Chase, Docomo, Hitachi, JD.com, KDDI, NVIDIA, Dell. J. L. is a Chan Zuckerberg Biohub investigator.

References


